LU 8.2 Is your polygon same as mine?

Introduction

Have you ever wondered how would you describe a triangle that is in your mind to somebody on a phone? What do you really tell, do you tell sides or angles? And is it possible, that the person would get the exact same figure that you had in mind? Moreover, how can you do that by giving minimum information? Today we will try to answer these questions by investigating some examples, making observations, and verifying or refuting these observations.

Task 1: Drawing your triangle Draw a triangle of your choice on the given blank sheet of paper. Measure the sides and the angles of the triangle and name the triangle. Now see triangles drawn by your friends. Do you see anything interesting? What is it?

Keep the paper safe, on which you drew your triangle, we will be coming back to this triangle later in the activity.

Task 2A: Constructing a triangle when one side is given

You know that only one side of the triangle is 6 cm. Now using this information draw a triangle on the given paper. Name your triangle.

triangle on the given paper. Name your triangle.						
Now study the triangle drawn by your partner.						
Is your triangle same as your partner's?						
How did you compare these two triangles?						

You and your partner both were given one angle of 55°. Did you both get exactly the same triangles? Why?

Task 2B: Constructing a triangle when one angle is given

You know that only one angle of the triangle is 55° . Now using this information draw a triangle on the given paper. Name your triangle.
Now study the triangle drawn by your partner. Is your triangle same as your partner's?
How did you compare these two triangles?
You and your partner both were given one angle of 55°. Did you both get exactly the same triangles? Why?
Task 3: Construct a triangle when two measures are given
Group A: Draw a triangle whose sides are 5 cm and 3 cm. Name your triangle.
Group B: Draw a triangle whose one side is 6 cm and one angle is 55°. Name your triangle.
Group C: Draw a triangle whose two angles are 50° and 75° . Name your triangle. Now study the triangle drawn by your partner.
Is your triangle same as your partner's?
How did you compare these two triangles?
Group A: You and your partner, both were given two sides, 5 cm, and 3 cm. Did you both get exactly the same triangles? Why?
Group B: You and your partner, both were given one side, 6 cm and one angle 55°.

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Did you both get exactly the same triangles? Why?

Group C:

Vigyan Pratibha Learning Unit If you think there are more than one ways to provide information such that a triangle, same as the one you drew in Task 1 could be constructed, please mention all those here.
Task 6: Constructing a quadrilateral
Now that you all know how to make a congruent triangle, let us figure out how to make a congruent quadrilateral. So if the minimum conditions for making a congruent triangle are three, what should be enough for a quadrilateral?
Now given that all the sides of a quadrilateral are 3 cm, think about all the different quadrilaterals that you can draw. Make the constructions on the given blank sheet. Did you or your partner get different quadrilaterals?
So if only sides are given, is it always possible to get different quadrilaterals? How do you know?
Imagine that you have to write to your friend about a quadrilateral. Now think of minimum information that you can send him/her, such that he/she gets the exact same quadrilateral as the one you had in your mind. What information you will send?
Think about why that set of information will lead to congruent or non-congruent quadrilaterals.
List the conditions that worked for constructing a unique quadrilateral.

Task 7:

We	have	found	out	the	minimum	infor	mation	needed	to	draw	congr	uent	triangles	and
con	gruent	t quad	rilate	erals	but let us	look	at son	ne specia	al tr	iangle	s and	quad	drilaterals	and
find	out w	hat kir	nd of	min	imum infoi	rmatio	on we n	eed to co	ons	truct t	hem.			

1. How many conditions do you need to construct congruent equilateral triangles?
2. How many pieces of information do you need to construct congruent squares?
3. How many pieces of information do you need to construct congruent rectangles?
4. How many pieces of information do you need to construct congruent rectangles?
5. How many pieces of information do you need to construct congruent parallelograms?
6. How many pieces of information do you need to construct congruent trapeziums?
Task 8: Constructing a pentagon Now that you all know how to make a congruent triangle or a congruent quadrilateral, let us figure out how to make a congruent pentagon. So if the minimum conditions for making a congruent triangle are three, and that for a quadrilateral are 5, what do you think the number of minimum conditions needed to construct a unique pentagon is?
Imagine that you have to write to your friend about a pentagon. Now think of minimum information that you can send him/her, such that he/she gets the exact same pentagon as the one you had in your mind. What information you will send?

Like in case of quadrilaterals for pentagons also there will be diagonals so 5 sides, 5 angles, and 5 diagonals, a total of 15 measures form the maximum information. Give students enough time to come up with combinations of information. Collect students' conjectures and lead the discussion for how it would work or not work.

Think pentag		why	that	set	of	information	will	lead	to	congruent	or	non-congruent
									· · · · · · · · · · · · · · · · · · ·			
List th	e condi	tions	that w	orke	d fo	or making a u	nique	e pent	ago	n.		
												

Task 9:

Now that you know the minimum conditions needed for making a congruent triangle and a congruent quadrilateral, let us explore how many conditions are needed for constructing a congruent hexagon, or a congruent heptagon.

Make some guesses, and make constructions on the given sheets of paper, record your guesses in the given table below.

Number of sides in the polygon	Name of the polygon	Minimum conditions required for constructing a congruent polygon
3	Triangle	3
4	Quadrilateral	5
5	Pentagon	
6	Hexagon	
7	Heptagon	
8	Octagon	

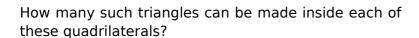
Table 1

Proving our understanding

Let us find out how can we prove which guesses are right and which ones are wrong.

Draw a quadrilateral.

Draw the first triangle inside the quadrilateral. See Figure 1 here. (Here we have drawn two different types of quadrilaterals)



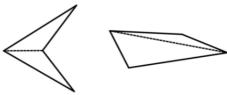


Figure 1

Yes, 2 such triangles can be made. We know that for constructing a congruent triangle we need 3 minimum conditions.

So in this case, to construct the first triangle we needed three minimum conditions. For the next triangle, we need three more, but as one side overlaps, you need only two conditions to construct triangle congruent to the second triangle. This also reconfirms with our understanding of minimum conditions no

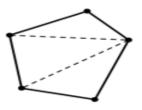


Figure 4

reconfirms with our understanding of minimum conditions needed for constructing a congruent quadrilateral.

What will happen if we do the same for a pentagon?

Let us draw a pentagon and see how many triangles can be made Inside a pentagon.

For the first triangle we need three conditions, for the second triangle we will need another 3 but then one side overlaps so we need only two. Similarly, for the third triangle, we need two more conditions.

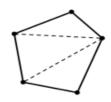


Figure 2

So you can see that whenever you add a triangle, you add two conditions. So the minimum conditions necessary for constructing a congruent pentagon, are 7 (3 + 2 + 2). But these five conditions give us a unique pentagon, hence the minimum pieces of information needed to construct a unique pentagon is 7.

Let us try to figure this octagons.	out for hexagons, heptagons, and					
How many triangles in a hexa	ngon?					
What is the minimum numbe unique hexagons?	er of conditions needed to construct Figure 3					
Why?	riguic 3					
How many triangles in a hept	agon?					
What is the minimum number of conditions needed to construct unique heptagon?						
Why?						
	How many triangles in an octagon?					
	What is the minimum number of conditions needed to construct congruent octagon?					
	Why?					
Figure 5						

References:

http://www.amesa.org.za/amesal_n21_a12.pdf https://www.mathopenref.com/congruentpolygons.html NCERT textbook Class 7 Chapter 7 NCERT textbook Class 8 Chapter 4